

# Optimal Estimation of Cloud Drop Effective Radius

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AAAR, Oct. 18th 2005

## Motivation

First aerosol indirect effect (IE):

increase in the number of cloud condensation nuclei  
generates a cloud with smaller drops (all else being equal).

To quantify IE, measure simultaneously cloud and aerosol properties:

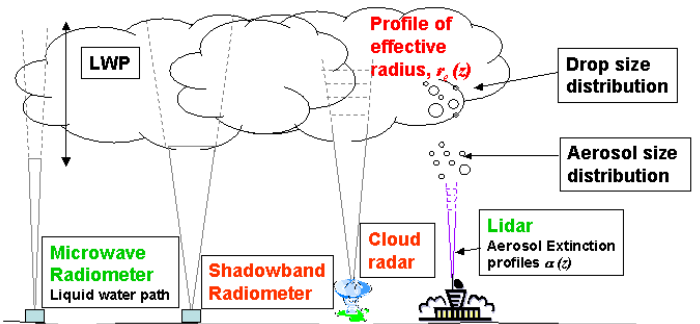
- (a) cloud drop effective radius ( $r_e$ ) and
- (b) cloud condensation nuclei (CCN) proxies.

Cloud drop radius  $r_e$  can be retrieved with different measurements:

- (a) Is there agreement between the techniques?
- (b) What is the "best" overall estimate of  $r_e$ ?

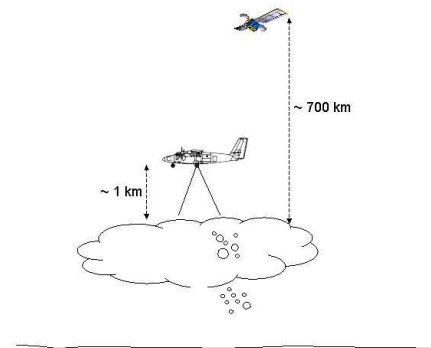
## Remote Sensing: Surface-based

Cloud radar, shadowband radiometer,  
(microwave radiometer, lidar, nephelometer)



## Remote Sensing: Space, Airborne

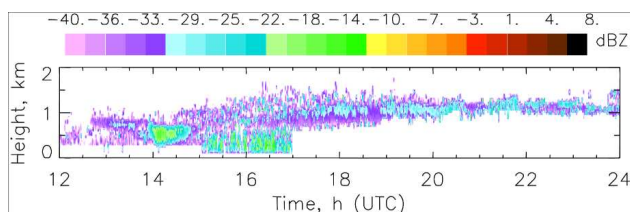
MODIS, flux radiometer, in situ probe



## Relevant Data for Optimal Estimation

On May 17 2003, single event during 'Intensive Operations Period' when 5 remote and in-situ drop size retrievals were available for comparison:

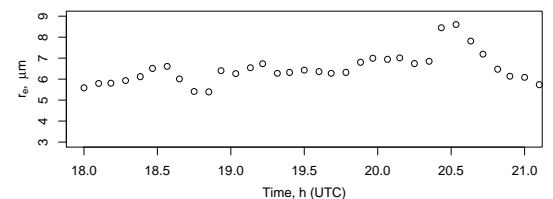
- Cloud radar (reflectivity)



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On May 17 2003, single event during 'Intensive Operations Period' when 5 remote and in-situ drop size retrievals were available for comparison:

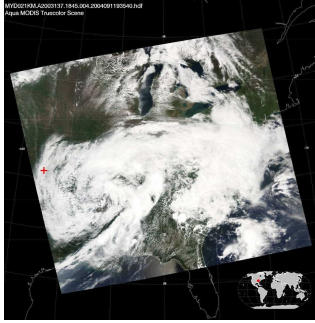
- Cloud radar
- Shadowband radiometer (derived  $r_e$ )



## Relevant Data for Optimal Estimation

On May 17 2003, single event during 'Intensive Operations Period' when 5 remote and in-situ drop size retrievals were available for comparison:

- Cloud radar
- Shadowband radiometer
- MODIS (cloud cover)

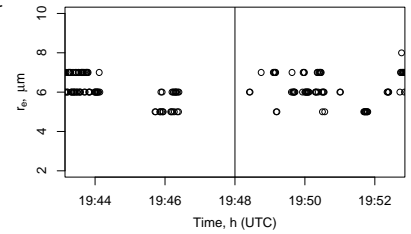


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## Relevant Data for Optimal Estimation

On May 17 2003, single event during 'Intensive Operations Period' when 5 remote and in-situ drop size retrievals were available for comparison:

- Cloud radar
- Shadowband radiometer
- MODIS
- Flux radiometer (derived  $r_e$ )

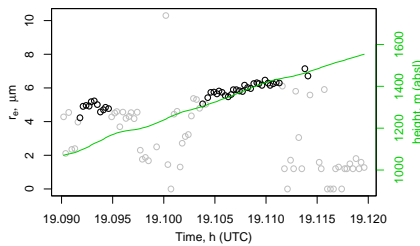


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## Relevant Data for Optimal Estimation

On May 17 2003, single event during 'Intensive Operations Period' when 5 remote and in-situ drop size retrievals were available for comparison:

- Cloud radar
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- In situ probe (derived  $r_e$ )



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## Data Summary

	Sampling period (s)	Sampling volume/ Footprint	Uncertainty in $r_e$ (%)
Cloud radar	20	700 m <sup>3</sup>	15 - 20
Shadowband radiometer	300	Circle of radius 1 km	13
MODIS	10 <sup>-4</sup>	2 km × 4.8 km	5 - 10
Flux radiometer	1	Circle of radius 2.7 km	15 - 20
In situ probe	1	7 cm <sup>3</sup>	15 - 20

Take into account: different sampling period  
different sampling volume  
different retrieval uncertainty

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## Best-estimate of $r_e$

Assume that for sufficiently small spatial and temporal scales,  $r_e$  does not change systematically.

Model  $r_e$  at height  $h$ , time  $t$  and horizontal location  $\mathbf{s}$  by

$$r_e(h, t, \mathbf{s}) = \theta_1 + \theta_2 h^{1/3} + \mathcal{Z}(h, t, \mathbf{s})$$

Mean zero Gaussian error process  $\mathcal{Z}$  with a complex variance structure.

Combine the different types of retrievals by accounting within  $\mathcal{Z}$  for

- sampling period,
- sampling volume,
- and retrieval uncertainty

to derive weighted least squares estimates for  $\theta_1$  and  $\theta_2$ .

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## Numerical Example

Data:

- Cloud radar: 688 data points between 19:20 and 19:50 (91 columns retrievals)
- Shadowband radiometer: 6 data points between 19:20 and 19:50
- MODIS: 3 × 3 square pixels centered at SGP site
- Flux radiometer: 3 data points between 19:47 and 19:49

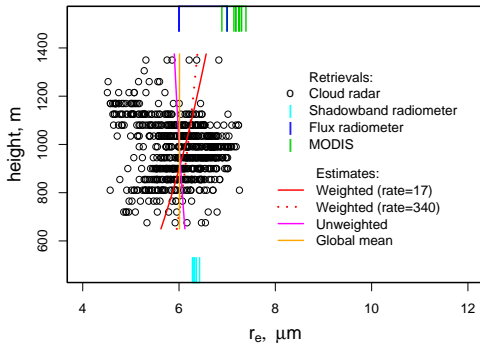
Weighting functions for spatial aggregation:

- Cloud radar: none, no spatial aggregation
- Shadowband radiometer: constant
- MODIS, flux radiometer: exponential with rates 17 or 340

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# Numerical Example: Best-Estimate

Superposition of all measurements and best-estimate profile of  $r_e$



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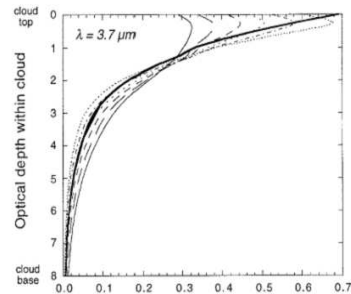
# Summary

- Comparison of five  $r_e$  retrieval methods on May 17 2003
- Methodology for deriving best-estimate of  $r_e(h, t, \mathbf{s})$ :
  - four remote sensors (shadowband radiometer, cloud radar, MODIS, flux radiometer)
  - incorporates uncertainties, weighting, different sampling volumes
- Calculation of IE for different  $r_e$  retrievals and different CCN proxies (radar, shadowband radiometer and lidar, nephelometer, PCASP):
  - even though  $r_e$  retrievals are similar, estimates of IE differ considerably
  - low statistics when binning by LWP

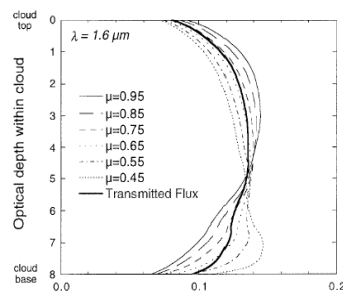
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# Weighting functions

Vertical weighting for reflectance



and for transmission



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# Addendum: IE

Simultaneously measure cloud and aerosol properties at surface

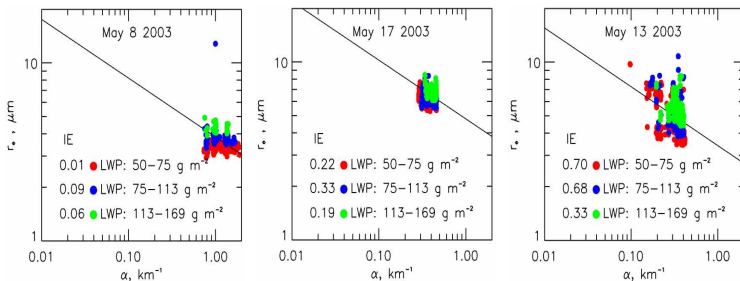
$$IE = -\frac{d \ln(r_e)}{d \ln(\text{CCN})} \quad 0 < IE < 0.33$$

- $r_e$ :
- Shadowband radiometer and microwave radiometer
  - Cloud radar and microwave radiometer
- CCN proxy:
- lidar extinction (355 nm; 350 m)
  - Nephelometer scattering (550 nm; surface)
  - PCASP aerosol concentration ( $>0.15 \mu\text{m}$ ; surface)

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# Addendum: IE

IE for 3 days with cloud radar and lidar extinction for CCN proxy



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# Addendum: IE

Calculations of IE for 3 LWP bins based on shadowband radiometer (MFRSR) or cloud radar (MMCR) and various CCN proxies. IE values should lie between 0 and 0.333. Note numerous excursions and even negative IE, when nephelometer is used as CCN proxy.

		LWP g m <sup>-2</sup>			
		50-75	75-113	113-169	
MFRSR	$r_e, \alpha$	All	1.07	-0.39	0.36
	$r_e, \sigma_{sp,g}$	All	-0.38	-0.23	0.36
	$r_e, N_a$	All	0.85	0.03	0.003
MMCR	$r_e, \alpha$	All	0.39	0.39	0.16
		May 8	0.01	0.09	0.06
		May 13	0.70	0.68	0.33
	$r_e, \sigma_{sp,g}$	May 17	0.22	0.33	0.19
		All	0.34	0.26	0.14
		May 8	0.03	-0.02	0.03
	$r_e, N_a$	May 13	-0.05	-0.16	0.10
		May 17	0.11	-0.16	-0.24
		All	0.94	0.80	1.55
		May 8	-	-	-
		May 13	-1.17	-2.40	-1.06
		May 17	0.05	0.22	0.36

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